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SCMPDS Is Not Standard

Artur Korniłowicz
University of Bialystok, Poland

Yasunari Shidama
Shinshu University, Nagano, Japan

Summary. The aim of the paper is to show that SCMPDS ([8]) does not belong to the class of standard computers ([16]).

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The articles [13], [19], [11], [3], [2], [14], [5], [12], [17], [1], [6], [9], [18], [20], [7], [4], [10], [15], [8], and [16] provide the notation and terminology for this paper.

1. Preliminaries

In this paper r, s are real numbers.

The following propositions are true:

(1) $0 \leq r + |r|$.

(2) $0 \leq -r + |r|$.

(3) If $|r| = |s|$, then $r = s$ or $r = -s$.

(4) For all natural numbers i, j such that $i < j$ and $i \neq 0$ holds $\frac{i}{j}$ is not integer.

(5) $\{2 \cdot k; k$ ranges over natural numbers: $k > 1\}$ is infinite.

(6) For every function f and for all sets a, b, c such that $a \neq c$ holds $(f {+\cdot} (a \dot{\longmapsto} b))(c) = f(c)$.

(7) For every function f and for all sets a, b, c, d such that $a \neq b$ holds $(f {+\cdot} [a \longmapsto c, b \longmapsto d])(a) = c$ and $(f {+\cdot} [a \longmapsto c, b \longmapsto d])(b) = d$.

2. SCMPDS

For simplicity, we use the following convention: a, b are Int positions, i is an instruction of SCMPDS, l is an instruction-location of SCMPDS, and k, k_1, k_2 are integers.

Let l_1, l_2 be Int positions and let a, b be integers. Then $[l_1 \longmapsto a, l_2 \longmapsto b]$ is a finite partial state of SCMPDS.

Let us note that SCMPDS has non trivial instruction locations.

Let l be an instruction-location of SCMPDS. The functor locnum(l) yields a natural number and is defined as follows:

(Def. 1) $\mathbf{i}_{\mathrm{locnum}(l)} = l$.

Let l be an instruction-location of SCMPDS. Then locnum(l) is a natural number.

The following propositions are true:

(8) $l = 2 \cdot \mathrm{locnum}(l) + 2$.

(9) For all instruction-locations l_3, l_4 of SCMPDS such that $l_3 \neq l_4$ holds $\mathrm{locnum}(l_3) \neq \mathrm{locnum}(l_4)$.

(10) For all instruction-locations l_3, l_4 of SCMPDS such that $l_3 \neq l_4$ holds $\mathrm{Next}(l_3) \neq \mathrm{Next}(l_4)$.

(11) Let N be a set with non empty elements, S be an IC-Ins-separated definite non empty non void AMI over N, i be an instruction of S, and l be an instruction-location of S. Then $\mathrm{JUMP}(i) \subseteq \mathrm{NIC}(i,l)$.

(12) If for every state s of SCMPDS such that $\mathbf{IC}_s = l$ and $s(l) = i$ holds $(\mathrm{Exec}(i,s))(\mathbf{IC}_{\mathrm{SCMPDS}}) = \mathrm{Next}(\mathbf{IC}_s)$, then $\mathrm{NIC}(i,l) = \{\mathrm{Next}(l)\}$.

(13) If for every instruction-location l of SCMPDS holds $\mathrm{NIC}(i,l) = \{\mathrm{Next}(l)\}$, then $\mathrm{JUMP}(i)$ is empty.

(14) $\mathrm{NIC}(\mathrm{goto}\, k, l) = \{2 \cdot |k + \mathrm{locnum}(l)| + 2\}$.

(15) $\mathrm{NIC}(\mathrm{return}\, a, l) = \{2 \cdot k; k$ ranges over natural numbers: $k > 1\}$.

(16) $\mathrm{NIC}(\mathrm{saveIC}(a,k_1), l) = \{\mathrm{Next}(l)\}$.

(17) $\mathrm{NIC}(a{:=}k_1, l) = \{\mathrm{Next}(l)\}$.

(18) $\mathrm{NIC}(a_{k_1}{:=}k_2, l) = \{\mathrm{Next}(l)\}$.

(19) $\mathrm{NIC}((a,k_1) := (b,k_2), l) = \{\mathrm{Next}(l)\}$.

(20) $\mathrm{NIC}(\mathrm{AddTo}(a,k_1,k_2), l) = \{\mathrm{Next}(l)\}$.

(21) $\mathrm{NIC}(\mathrm{AddTo}(a,k_1,b,k_2), l) = \{\mathrm{Next}(l)\}$.

(22) $\mathrm{NIC}(\mathrm{SubFrom}(a,k_1,b,k_2), l) = \{\mathrm{Next}(l)\}$.

(23) $\mathrm{NIC}(\mathrm{MultBy}(a,k_1,b,k_2), l) = \{\mathrm{Next}(l)\}$.

(24) $\mathrm{NIC}(\mathrm{Divide}(a,k_1,b,k_2), l) = \{\mathrm{Next}(l)\}$.

(25) $\mathrm{NIC}((a,k_1) <> 0\_\mathrm{goto}\, k_2, l) = \{\mathrm{Next}(l), |2 \cdot (k_2 + \mathrm{locnum}(l))| + 2\}$.

(26) $\mathrm{NIC}((a,k_1) <= 0\_\mathrm{goto}\, k_2, l) = \{\mathrm{Next}(l), |2 \cdot (k_2 + \mathrm{locnum}(l))| + 2\}$.

(27) $\mathrm{NIC}((a,k_1) >= 0\_\mathrm{goto}\, k_2, l) = \{\mathrm{Next}(l), |2 \cdot (k_2 + \mathrm{locnum}(l))| + 2\}$.

Let us consider k. Observe that $\mathrm{JUMP}(\mathrm{goto}\, k)$ is empty.
One can prove the following proposition

(28) $\mathrm{JUMP}(\mathrm{return}\, a) = \{2 \cdot k; k$ ranges over natural numbers: $k > 1\}$.

Let us consider a. One can verify that $\mathrm{JUMP}(\mathrm{return}\, a)$ is infinite.
Let us consider a, k_1. Observe that $\mathrm{JUMP}(\mathrm{saveIC}(a,k_1))$ is empty.
Let us consider a, k_1. One can check that $\mathrm{JUMP}(a{:=}k_1)$ is empty.
Let us consider a, k_1, k_2. Observe that $\mathrm{JUMP}(a_{k_1}{:=}k_2)$ is empty.
Let us consider a, b, k_1, k_2. One can verify that $\mathrm{JUMP}((a,k_1) := (b,k_2))$ is empty.
Let us consider a, k_1, k_2. Observe that $\mathrm{JUMP}(\mathrm{AddTo}(a,k_1,k_2))$ is empty.
Let us consider a, b, k_1, k_2. One can verify the following observations:

* $\mathrm{JUMP}(\mathrm{AddTo}(a,k_1,b,k_2))$ is empty,
* $\mathrm{JUMP}(\mathrm{SubFrom}(a,k_1,b,k_2))$ is empty,
* $\mathrm{JUMP}(\mathrm{MultBy}(a,k_1,b,k_2))$ is empty, and
* $\mathrm{JUMP}(\mathrm{Divide}(a,k_1,b,k_2))$ is empty.

Let us consider a, k_1, k_2. One can check the following observations:

* JUMP$((a,k_1) <> 0_\mathrm{goto}\, k_2)$ is empty,
* JUMP$((a,k_1) <= 0_\mathrm{goto}\, k_2)$ is empty, and
* JUMP$((a,k_1) >= 0_\mathrm{goto}\, k_2)$ is empty.

Next we state two propositions:

(29) SUCC(l) = the instruction locations of SCMPDS.

(30) Let N be a set with non empty elements, S be an IC-Ins-separated definite non empty non void AMI over N, and l_3, l_4 be instruction-locations of S. If SUCC(l_3) = the instruction locations of S, then $l_3 \leq l_4$.

Let us observe that SCMPDS is non InsLoc-antisymmetric.
Let us note that SCMPDS is non standard.

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